Pre-AP Calculus



MULTIPLE CHOICE – Calculator NOT Permitted

1. Which of the following would be the equation for the circle pictured to the right?

A. $x^{2} - 4x + y^{2} + 2y - 4 = 0$ B. $x^{2} - 4x + y^{2} - 2y - 4 = 0$ C. $x^{2} + 4x + y^{2} + 2y - 4 = 0$ D. $x^{2} - 4x + y^{2} + 2y - 9 = 0$ E. $x^{2} + 4x + y^{2} - 2y - 4 = 0$

2. Which of the following equations would define the semi-circle pictured to the right?

A.
$$y = -1 - \sqrt{16 - (x+3)^2}$$

B. $x = 3 - \sqrt{16 - (y+1)^2}$
C. $y = 1 - \sqrt{16 - (x-3)^2}$
D. $x = 3 + \sqrt{16 - (y+1)^2}$
E. $x = 3 - \sqrt{16 - (y-1)^2}$





- 4. The graph of an ellipse is pictured to the right. Which of the following points is/are foci of the ellipse?
 - I. $(-2, -2+2\sqrt{3})$ II. $(-2+2\sqrt{3}, -2)$ III. $(-2-2\sqrt{3}, -2)$ A. I only B. II only C. III only D. I and II only E. II and III only
 - 5. Find the equation of an ellipse whose vertices are (1, 6) and (1, -2) and has a minor axis whose length is 6.

A.
$$\frac{(x-1)^2}{9} + \frac{(y-2)^2}{16} = 1$$

B. $\frac{(x+1)^2}{3} + \frac{(y+2)^2}{4} = 1$
C. $\frac{(x-1)^2}{6} + \frac{(y-2)^2}{8} = 1$
D. $\frac{(x+1)^2}{16} + \frac{(y+2)^2}{9} = 1$
E. $\frac{(x-1)^2}{36} + \frac{(y-2)^2}{16} = 1$

- 6. The equation of a circle is $(x + 2)^2 + (y + 3)^2 = 4$. The line y = x 1...
 - A. intersects the circle at only one point.
 - B. does not intersect the circle at any points.
 - C. intersects the circle at exactly two points and passes through the center.
 - D. intersects the circle at exactly two points and does not pass through the center.



3. An ellipse is defined by the equation $4(x + 3)^2 + 9(v - 2)^2 = 36$. Which of

- II. The co-vertices of the ellipse are (-3, 4) and (-3, 0).
- III. The major axis is horizontal and has a length of 6.
- A. I only B. II only

the following statements is/are true about the graph?

D. I and III only E. III only



C. II and III only







- 7. Find the distance from the center of the circle defined by the equation $x^2 + 6x + y^2 4y 12 = 0$ and the negative zero of the quadratic function $g(x) = 2x^2 + 7x 15$.
 - A. $2\sqrt{2}$ B. $2\sqrt{17}$ C. $2\sqrt{15}$
 - D. $\sqrt{13}$ E. 17

- 8. Which of the following equations, when graphed, is/are circles?
 - I. $2(x+3)^2 2(y+2)^2 = 1$ II. $2(x-3)^2 + (y-1)^2 = 4$ III. $x^2 + y^2 - 8x + 4y - 25 = 0$
 - A. I and II onlyB. II onlyC. II and III onlyD. I and III onlyE. III only
- 9. Which of the following is an equation of the graphed ellipse?
 - A. $\frac{x^2}{16} \frac{(y+1)^2}{9} = 1$ B. $\frac{x^2}{4} + \frac{(y+1)^2}{3} = 1$ C. $\frac{x^2}{16} + \frac{(y-1)^2}{9} = 1$ D. $\frac{x^2}{4} + \frac{(y-1)^2}{3} = 1$ E. $\frac{x^2}{16} + \frac{(y+1)^2}{9} = 1$





- 10. Which of the following equations would be the correct equation for the hyperbola pictured to the right?
 - A. $\frac{(x+3)^2}{4} + \frac{(y-1)^2}{9} = 1$ B. $\frac{(x+3)^2}{2} - \frac{(y-1)^2}{3} = 1$ C. $\frac{(x+3)^2}{4} - \frac{(y-1)^2}{9} = 1$ D. $\frac{(x-3)^2}{4} - \frac{(y+1)^2}{9} = 1$

11. Which of the following statement equation $\frac{(y+4)^2}{8} - \frac{(x-2)^2}{9} = 1?$	ents is/are true about the graph o	of the hyperbola defined by the						
I. The transverse axis of the hyperbola is the y – axis.								
II. The slopes of the asymptotes of the graph are $\pm \frac{2}{3}\sqrt{2}$.								
III. One of the vertices of the hyperbola has coordinates $(2, -4 - 2\sqrt{2})$								
A. I and III only	B. I only	C. I and II only						
D. I, II, and III	E. II only							
12. The equation $y^2 + 4x^2 = 2x $ would have a graph that displayed which of the following types of symmetry?								
I. $x - axis$	II. $y - axis$	III. origin						
A. I and II only	B. I, II and III	C. I only						
D. II only	E. III only							
	Free Response							
Given below are three implicitly def questions that follow.	fined equations whose graphs re	present conic sections. Answer the						

Equation I	Equation II	Equation III
$4y^2 - x^2 + 8y - 4x - 4 = 0$	$2x^2 + 4x + 2y^2 - 16y - 16 = 0$	$9x^2 + 4y^2 + 36x - 8y + 4 = 0$

a. When each equation is graphed, which conic section will be formed by each equation? Justify your reasoning for each based on the equation in its given form above.

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b.	Find the area of the circle represented by the equation you identified as being a circle in part a).	Show
	your work, leaving your answer in terms of π .	

c.	Graph the hyperbola defined by the equation from part a) that you identified, indicating the characteristics below.						
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	Intersection of the Asymptotes:						
	Slope of the Asymptotes:	8 -	7 -	6 -	5 -	1 _	3
	Coordinates of the Vertices:			·			••••

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