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## SHOW WORK ON A SEPARATE SHEET, IF NECESSARY:

1. Which of the following has a radius less than 5 inches? Circle the letter of all that apply.
(A) a cylindrical can with a volume of 424.12 cubic inches and a height of 15 inches
(B) a cylindrical can with a volume of 565.49 cubic inches and a height of 5 inches
(C) a cone with a volume of 201.06 cubic inches and a height of 12 inches
(D) a cone with a volume of 254.47 cubic inches and a height of 12 inches
2. A company produces bags of chips. The acceptable weight of a bag can be expressed by $|x-250| \leq 0.8$, where x is the weight of the bag of chips in grams.
Circle the letters of all the statements that are true.
(A) a bag of chips that weighs 251 grams is acceptable
(B) the difference between the maximum and minimum acceptable weights is 1.6 gram
(C) the minimum acceptable weight of a bag of chips is 249.8 grams
(D) a bag of chips that weighs 249.55 grams is acceptable
3. A chord with length $L$ is drawn in a circle. Which equation will find the smallest distance, $x$, from the chord to the center of the circle if $r$ is the radius of the circle?
(A) $L=\sqrt{r^{2}-x^{2}}$
(B) $L=\sqrt{r^{2}+x^{2}}$
(C) $L=2 \sqrt{r^{2}-x^{2}}$
(D) $L=2 \sqrt{r^{2}+x^{2}}$
4. Circles $M, P$, and $Q$ are tangent to line $l$ and to each other as shown in the diagram on the right. Circles $M$ and $Q$ have the same radius. What is the ratio of the radius of circle $M$ to the radius of circle $P$ ?
(A) $3: 1$
(B) $4: 1$
(C) $5: 1$
(D) $6: 1$

Figure for \#5:

6. A chord with a length of $c$ units is drawn in a circle with a radius of $r$ units. Which equation will find the shortest distance, $x$, from the center of the circle to the chord?
(A) $x=\sqrt{r^{2}-\frac{c^{2}}{2}}$
(B) $x=\sqrt{r^{2}-\frac{c^{2}}{4}}$
(C) $x=\sqrt{c^{2}-\frac{r^{2}}{2}}$
(D) $x=\sqrt{c^{2}-\frac{r^{2}}{4}}$
7. A company wants to conduct a survey of its clients about the product warranty it provides.

* The company has 8,000 clients.
* It plans to survey a total of 200 clients.

Which method would provide the company with a simple random sample?
(A) asking the first 200 clients who order its product on a random day
(B) picking the first 40 clients who order its product each day for 5 days
(C) numbering all of the clients from 1 to 8,000 and using a random number generator to select 200 clients
(D) starting with the $40^{\text {th }}$ client's account and taking every $20^{\text {th }}$ account until 200 clients have been chosen
9. A company wants to learn more about what customers think about the services it offers. Which procedure is most likely to produce an unbiased sample?
(A) surveying the first 100 people that call the company
(B) looking at reviews about the company on the Internet
(C) asking 100 customers from the end of an alphabetized list to complete a phone survey
(D) surveying a random sample of customers from a list of all customers
11. The graph of a quadratic function has its vertex at $\left(\frac{3}{4}, \frac{25}{8}\right)$. The $y$-intercept is 2 . What is the distance, in units, between the two $x$-intercepts of the function?
12. Identify the type of study that best describes each scenario below as: Survey, Observation, Experiment

A student participating in a school science fair wants to determine whether a flower will grow faster in direct sunlight. She randomly assigned half of the plants to receive direct sunlight and the other half to a dimly lit room and the growth of each plant is tracked for 6 weeks.

A local toy store conducts an investigation to determine whether right-handed people can assemble a 25 -piece puzzle quicker than left-handed people. The puzzle is left out for customers to play with. When a customer plays with the puzzle, thee customer's handedness and time to complete the puzzle are recorded.

A principal questions a random sample of 100 students walking through the halls to determine the average number of hours of sleep a student gets each night.
13. A cubic equation has a zero at -2 and $\frac{1}{3}$ and a factor of $(x+1)$. It has a relative maximum at about ( $-1.56,1.4$ ). Circle one option from each of the lists below to create an equation that meets those criteria.

| $y=$ | $2 x^{3}$ | $+8 x^{2}$ | $+3 x$ | +6 |
| :---: | :---: | :---: | :---: | :---: |
|  | $-8 x^{2}$ | $-3 x$ | -6 |  |
|  | $3 x^{3}$ | $+10 x^{2}$ | $+9 x$ | +2 |
|  | $-3 x^{3}$ | $-10 x^{2}$ | $-9 x$ | -2 |

14. The equation $5 \cdot\left(\frac{1}{3}\right)^{(3 x-1)}=10$ is rewritten in the form $\log _{b} d=c$. Find $b, d$, and $c$.
15. The function $f(x)=\frac{3}{x}$ is shifted 7 units to the right and 4 units up, creating $g(x)=\frac{3}{x+h}+k$. What is the value of $h+k$ ?
16. The height of the water at the end of a pier is monitored.

* The average height of the water is 10.8 feet.
* The height of the water varies by as much as 8 feet during any 24 -hour day.
* High tide occurs at 5:30 p.m., with the water returning to its average height at 8:30 p.m.
Which function gives the height, $H$, of the water as a function of time, $t$, in hours, where $t=0$ at 8:30 p.m.?
(A) $H(t)=-4 \sin \left(\frac{\pi}{12} t\right)+10.8$
(B) $H(t)=-4 \sin \left(\frac{\pi}{6} t\right)+10.8$
(C) $H(t)=4 \sin \left(\frac{\pi}{12} t\right)+10.8$
(D) $H(t)=4 \sin \left(\frac{\pi}{6} t\right)+10.8$

16. A school wants to find out which new lunch choice its students would prefer. Which is most likely to obtain a statistically unbiased sample?
(A) surveying a random sample of students from a list of all students
(B) inviting all students to indicate their choice with a text message
(C) placing suggestion boxes at random locations in the school
(D) assembling a group with one male and one female student from each grade and recording the preferences of these students
17. Which expression is equivalent to $\left(x^{2}+5 x-19\right) \div\left(x^{2}+7 x+8\right) ?$
(A) $1+\frac{12 x-11}{x^{2}+7 x+8}$
(B) $1-\frac{12 x-11}{x^{2}+7 x+8}$
(C) $1+\frac{2 x+27}{x^{2}+7 x+8}$
(D) $1-\frac{2 x+27}{x^{2}+7 x+8}$
18. What are the zeros of the function $x^{4}-2 x^{3}+x^{2}-8 x-12=0$ ?
(A) $-1,-3, \pm 2 i$
(B) $-1,-3, \pm 3 i$
(C) $-1,3, \pm 2 i$
(D) $-1,3, \pm 3 i$
19. What is the remainder for $\left(x^{3}-13 x-15\right) \div(x+2) ?$
(A) 3
(B) -37
(C) -33
(D) -45
20. What are the zeros of the function $15 x^{4}+19 x^{3}-54 x^{2}-76 x-24=0$ ?
(A) $\pm 2, \frac{2}{3}, \frac{-3}{5}$
(B) $\pm 2, \frac{-2}{3}, \frac{-3}{5}$
(C) $\pm 1, \frac{-2}{3}, \frac{3}{5}$
(D) $\pm 1,2, \frac{-2}{3}$
21. Which equation describes the graph that is produced by moving $y=|x|$ to the left 3 and up 2 units?
(A) $y=|x+3|-2$
(B) $y=|x+3|+2$
(C) $y=|x-3|-2$
(D) $y=|x-3|+2$
22. An empty cone-shaped container has a diameter of 5 inches at the top.

* The height of the container is 8 inches.
* James pours water into the container until the surface of the water is 2 inches below the top of the container.

What volume, to the nearest hundredth of a cubic inch, of water did James pour into the container?
24. What are the zeros of $f(x)=2 x^{2}+x-1$ ?
(A) $\frac{-1}{2}$ and 1
(B) $\frac{1}{2}$ and -1
(C) $\frac{-2}{3}$ and 3
(D) $\frac{2}{3}$ and -3
25. If $f(x)=2 x^{2}-5 x-12$ and $f(4)=0$, which statement is true?
(A) $2 x+13$ is a factor of $f(x)$.
(B) $2 x-13$ is a factor of $f(x)$.
(C) $2 x+3$ is a factor of $f(x)$.
(D) $2 x-3$ is a factor of $f(x)$.

