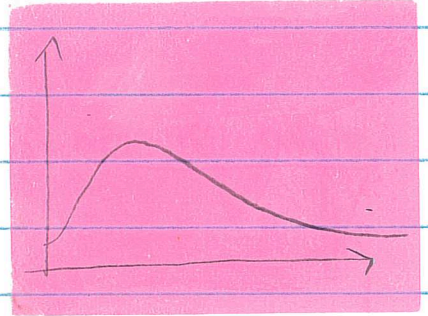


## Unit 8 - $\chi^2$ Homogeneity and Independence tests

We use  $\chi^2$  tests to observe if different variables are independent or dependent, and homogeneous/heterogeneous

Chi-Squared Dist:

- Almost Always right skewed
- Gets more normal as sample size goes up



Always do CHAD (conditions, hypothesis, alpha, dof)

### Conditions

- random says
- normal  $n \cdot p \geq 5$  for all expected values
- Independent  $n < 1N$

### Dof

1 Var:  $(\# \text{ columns} - 1)$   
2 vars:  $(\text{rows} - 1) \cdot (\text{columns} - 1)$

$\alpha$  = usually .05

unless says otherwise

### Hypotheses

$H_0$ : <sup>homo</sup>no differ dist, <sup>independence</sup>no association  
 $H_a$ : differ dist, association

### Differences of Homogeneous and Independent

homogeneous -

- Compares 1 variable across 2 populations
- Asks if difference in the distribution of populations

Independent -

- Compares 2 variables for one population
- Asks if association between 2 variables in a population

### Main order of steps

1. Find expected values, plug in obs data L1, exp data L2
2. CHAD, plug lists into formula, Sto  $\rightarrow$  L3, Stats Calc vars on L3, Look at  $\chi^2$ . That's the test statistic  $\rightarrow$  2nd vars  $\chi^2$  cdf, <sup>compare</sup> p-value

## Calculating $\chi^2$

Expected values -

- If %'s, multiply each % by the total sample size.
- If table, do  $\frac{(\text{row total} \cdot \text{column total})}{\text{total}}$

Ex)

	kayak	bike	raft	
NOC	79 observed			720
WW				
Gorge				
	123			1745

To find the expected # of kayakers at NOC, do:

$$\left( \frac{720 \cdot 123}{1745} \right)$$

• Plug obs into  $L_1$ , expected into  $L_2$

$$\chi^2 = \sum \frac{(\text{obs} - \text{exp})^2}{\text{exp}} \quad \text{So...} \quad L_3 = \frac{(L_1 - L_2)^2}{L_2}$$

Sto that into  $L_3$ , then calc  $L_3$  and  $\sum x$  is test stat.

Convert to p-value!  $\sum x \rightarrow$  2nd vars, #8  $\chi^2$  cdf.

If  $p > \alpha$  not reject null, if  $p < \alpha$  reject null

results not significant; accept alt of associated  
no association between vars; or difference in dist. of  
or no difference in dist. of populations.  
of populations

## Residuals - part of unit 9

• It is possible to make residual points from  $L_2 - L_3$  or (obs - exp)

To get  $L_3$ :  $y = \text{slope}(L_1) + y\text{-int}$ . This gives expected values of LSRL. This tests if the LSRL is a good fit. Do  $(L_1, L_4)$  as residual points. If no pattern, linear is good fit.